

ANSWERS/HINTS

EXERCISE 1.1

- (i) $2^2 \times 5 \times 7$ (ii) $2^2 \times 3 \times 13$ (iii) $3^2 \times 5^2 \times 17$
(iv) $5 \times 7 \times 11 \times 13$ (v) $17 \times 19 \times 23$
- (i) LCM = 182; HCF = 13 (ii) LCM = 23460; HCF = 2 (iii) LCM = 3024; HCF = 6
- (i) LCM = 420; HCF = 3 (ii) LCM = 11339; HCF = 1 (iii) LCM = 1800; HCF = 1
- 22338 7. 36 minutes

EXERCISE 2.1

- (i) No zeroes (ii) 1 (iii) 3 (iv) 2 (v) 4 (vi) 3

EXERCISE 2.2

- (i) -2, 4 (ii) $\frac{1}{2}, \frac{1}{2}$ (iii) $-\frac{1}{3}, \frac{3}{2}$
(iv) -2, 0 (v) $-\sqrt{15}, \sqrt{15}$ (vi) $-1, \frac{4}{3}$
- (i) $4x^2 - x - 4$ (ii) $3x^2 - 3\sqrt{2}x + 1$ (iii) $x^2 + \sqrt{5}$
(iv) $x^2 - x + 1$ (v) $4x^2 + x + 1$ (vi) $x^2 - 4x + 1$

EXERCISE 3.1

- (i) Required pair of linear equations is
 $x + y = 10$; $x - y = 4$, where x is the number of girls and y is the number of boys.
To solve graphically draw the graphs of these equations on the same axes on graph paper.
Girls = 7, Boys = 3.

(ii) Required pair of linear equations is

$5x + 7y = 50$; $7x + 5y = 46$, where x and y represent the cost (in ₹) of a pencil and of a pen respectively.

To solve graphically, draw the graphs of these equations on the same axes on graph paper.

Cost of one pencil = ₹ 3, Cost of one pen = ₹ 5

2. (i) Intersect at a point (ii) Coincident (iii) Parallel
3. (i) Consistent (ii) Inconsistent (iii) Consistent
- (iv) Consistent (v) Consistent
4. (i) Consistent (ii) Inconsistent (iii) Consistent (iv) Inconsistent
- The solution of (i) above, is given by $y = 5 - x$, where x can take any value, i.e., there are infinitely many solutions.
- The solution of (iii) above is $x = 2, y = 2$, i.e., unique solution.
5. Length = 20 m and breadth = 16 m.
6. One possible answer for the three parts:
- (i) $3x + 2y - 7 = 0$ (ii) $2x + 3y - 12 = 0$ (iii) $4x + 6y - 16 = 0$
7. Vertices of the triangle are $(-1, 0)$, $(4, 0)$ and $(2, 3)$.

EXERCISE 3.2

1. (i) $x = 9, y = 5$ (ii) $s = 9, t = 6$ (iii) $y = 3x - 3$,
where x can take any real value, i.e., infinitely many solutions.
- (iv) $x = 2, y = 3$ (v) $x = 0, y = 0$ (vi) $x = 2, y = 3$
2. $x = -2, y = 5; m = -1$
3. (i) $x - y = 26, x = 3y$, where x and y are two numbers ($x > y$); $x = 39, y = 13$.
- (ii) $x - y = 18, x + y = 180$, where x and y are the measures of the two angles in degrees; $x = 99, y = 81$.
- (iii) $7x + 6y = 3800, 3x + 5y = 1750$, where x and y are the costs (in ₹) of one bat and one ball respectively; $x = 500, y = 50$.
- (iv) $x + 10y = 105, x + 15y = 155$, where x is the fixed charge (in ₹) and y is the charge (in ₹ per km); $x = 5, y = 10$; ₹ 255.
- (v) $11x - 9y + 4 = 0, 6x - 5y + 3 = 0$, where x and y are numerator and denominator of the fraction; $\frac{7}{9}$ ($x = 7, y = 9$).
- (vi) $x - 3y - 10 = 0, x - 7y + 30 = 0$, where x and y are the ages in years of Jacob and his son; $x = 40, y = 10$.

EXERCISE 3.3

1. (i) $x = \frac{19}{5}, y = \frac{6}{5}$ (ii) $x = 2, y = 1$ (iii) $x = \frac{9}{13}, y = -\frac{5}{13}$
 (iv) $x = 2, y = -3$
2. (i) $x - y + 2 = 0, 2x - y - 1 = 0$, where x and y are the numerator and denominator of the fraction; $\frac{3}{5}$.
 (ii) $x - 3y + 10 = 0, x - 2y - 10 = 0$, where x and y are the ages (in years) of Nuri and Sonu respectively. Age of Nuri (x) = 50, Age of Sonu (y) = 20.
 (iii) $x + y = 9, 8x - y = 0$, where x and y are respectively the tens and units digits of the number; 18.
 (iv) $x + 2y = 40, x + y = 25$, where x and y are respectively the number of ₹ 50 and ₹ 100 notes; $x = 10, y = 15$.
 (v) $x + 4y = 27, x + 2y = 21$, where x is the fixed charge (in ₹) and y is the additional charge (in ₹) per day; $x = 15, y = 3$.

EXERCISE 4.1

1. (i) Yes (ii) Yes (iii) No (iv) Yes
 (v) Yes (vi) No (vii) No (viii) Yes
2. (i) $2x^2 + x - 528 = 0$, where x is breadth (in metres) of the plot.
 (ii) $x^2 + x - 306 = 0$, where x is the smaller integer.
 (iii) $x^2 + 32x - 273 = 0$, where x (in years) is the present age of Rohan.
 (iv) $u^2 - 8u - 1280 = 0$, where u (in km/h) is the speed of the train.

EXERCISE 4.2

1. (i) $-2, 5$ (ii) $-2, \frac{3}{2}$ (iii) $-\frac{5}{\sqrt{2}}, -\sqrt{2}$
 (iv) $\frac{1}{4}, \frac{1}{4}$ (v) $\frac{1}{10}, \frac{1}{10}$
2. (i) 9, 36 (ii) 25, 30
3. Numbers are 13 and 14. 4. Positive integers are 13 and 14.
5. 5 cm and 12 cm 6. Number of articles = 6, Cost of each article = ₹ 15

EXERCISE 4.3

1. (i) Real roots do not exist (ii) Equal roots; $\frac{2}{\sqrt{3}}, \frac{2}{\sqrt{3}}$ (iii) Distinct roots; $\frac{3 \pm \sqrt{3}}{2}$
 2. (i) $k = \pm 2\sqrt{6}$ (ii) $k = 6$
 3. Yes. 40 m, 20 m 4. No 5. Yes. 20 m, 20 m

EXERCISE 5.1

1. (i) Yes. 15, 23, 31, ... forms an AP as each succeeding term is obtained by adding 8 in its preceding term.
 (ii) No. Volumes are $V, \frac{3V}{4}, \left(\frac{3}{4}\right)^2 V, \dots$ (iii) Yes. 150, 200, 250, ... form an AP.
 (iv) No. Amounts are $10000\left(1 + \frac{8}{100}\right), 10000\left(1 + \frac{8}{100}\right)^2, 10000\left(1 + \frac{8}{100}\right)^3, \dots$
2. (i) 10, 20, 30, 40 (ii) $-2, -2, -2, -2$ (iii) 4, 1, $-2, -5$
 (iv) $-1, -\frac{1}{2}, 0, \frac{1}{2}$ (v) $-1.25, -1.50, -1.75, -2.0$
3. (i) $a = 3, d = -2$ (ii) $a = -5, d = 4$
 (iii) $a = \frac{1}{3}, d = \frac{4}{3}$ (iv) $a = 0.6, d = 1.1$
4. (i) No (ii) Yes. $d = \frac{1}{2}; 4, \frac{9}{2}, 5$
 (iii) Yes. $d = -2; -9.2, -11.2, -13.2$ (iv) Yes. $d = 4; 6, 10, 14$
 (v) Yes. $d = \sqrt{2}; 3 + 4\sqrt{2}, 3 + 5\sqrt{2}, 3 + 6\sqrt{2}$ (vi) No
 (vii) Yes. $d = -4; -16, -20, -24$ (viii) Yes. $d = 0; -\frac{1}{2}, -\frac{1}{2}, -\frac{1}{2}$
 (ix) No (x) Yes. $d = a; 5a, 6a, 7a$
 (xi) No (xii) Yes. $d = \sqrt{2}; \sqrt{50}, \sqrt{72}, \sqrt{98}$
 (xiii) No (xiv) No (xv) Yes. $d = 24; 97, 121, 145$

EXERCISE 5.2

1. (i) $a_n = 28$ (ii) $d = 2$ (iii) $a = 46$ (iv) $n = 10$ (v) $a_n = 3.5$

2. (i) C (ii) B
3. (i) $\boxed{14}$ (ii) $\boxed{18}, \boxed{8}$ (iii) $\boxed{6\frac{1}{2}}, \boxed{8}$
 (iv) $\boxed{-2}, \boxed{0}, \boxed{2}, \boxed{4}$ (v) $\boxed{53}, \boxed{23}, \boxed{8}, \boxed{-7}$
4. 16th term 5. (i) 34 (ii) 27
6. No 7. 178 8. 64
9. 5th term 10. 1 11. 65th term
12. 100 13. 128 14. 60
15. 13 16. 4, 10, 16, 22, ...
17. 20th term from the last term is 158.
18. -13, -8, -3 19. 11th year 20. 10

EXERCISE 5.3

1. (i) 245 (ii) -180 (iii) 5505 (iv) $\frac{33}{20}$
2. (i) $1046\frac{1}{2}$ (ii) 286 (iii) -8930
3. (i) $n = 16, S_n = 440$ (ii) $d = \frac{7}{3}, S_{13} = 273$ (iii) $a = 4, S_{12} = 246$
 (iv) $d = -1, a_{10} = 8$ (v) $a = -\frac{35}{3}, a_9 = \frac{85}{3}$ (vi) $n = 5, a_n = 34$
 (vii) $n = 6, d = \frac{54}{5}$ (viii) $n = 7, a = -8$ (ix) $d = 6$
 (x) $a = 4$
4. 12. By putting $a = 9, d = 8, S = 636$ in the formula $S = \frac{n}{2}[2a + (n - 1)d]$, we get a quadratic equation $4n^2 + 5n - 636 = 0$. On solving, we get $n = -\frac{53}{4}, 12$. Out of these two roots only one root 12 is admissible.
5. $n = 16, d = \frac{8}{3}$ 6. $n = 38, S = 6973$ 7. Sum = 1661
8. $S_{51} = 5610$ 9. n^2 10. (i) $S_{15} = 525$ (ii) $S_{15} = -465$

11. $S_1 = 3, S_2 = 4; a_2 = S_2 - S_1 = 1; S_3 = 3, a_3 = S_3 - S_2 = -1,$
 $a_{10} = S_{10} - S_9 = -15; a_n = S_n - S_{n-1} = 5 - 2n.$
12. 4920 13. 960 14. 625 15. ₹ 27750
16. Values of the prizes (in ₹) are 160, 140, 120, 100, 80, 60, 40.
17. 234 18. 143 cm
19. 16 rows, 5 logs are placed in the top row. By putting $S = 200, a = 20, d = -1$ in the formula
 $S = \frac{n}{2}[2a + (n - 1)d],$ we get, $41n - n^2 = 400.$ On solving, $n = 16, 25.$ Therefore, the
 number of rows is either 16 or 25. $a_{25} = a + 24d = -4$
 i.e., number of logs in 25th row is -4 which is not possible. Therefore $n = 25$ is not
 possible. For $n = 16, a_{16} = 5.$ Therefore, there are 16 rows and 5 logs placed in the top
 row.
20. 370m

EXERCISE 5.4 (Optional)*

1. 32nd term 2. $S_{16} = 20, 76$ 3. 385 cm
 4. 35 5. 750 m^3

EXERCISE 6.1

1. (i) Similar (ii) Similar (iii) Equilateral
 (iv) Equal, Proportional 3. No

EXERCISE 6.2

1. (i) 2 cm (ii) 2.4 cm
 2. (i) No (ii) Yes (iii) Yes
 9. Through O, draw a line parallel to DC, intersecting AD and BC at E and F respectively.

EXERCISE 6.3

1. (i) Yes. AAA, $\Delta ABC \sim \Delta PQR$ (ii) Yes. SSS, $\Delta ABC \sim \Delta QRP$
 (iii) No (iv) Yes. SAS, $\Delta MNL \sim \Delta QPR$
 (v) No (vi) Yes. AA, $\Delta DEF \sim \Delta PQR$
2. $55^\circ, 55^\circ, 55^\circ$
14. Produce AD to a point E such that $AD = DE$ and produce PM to a point N such that
 $PM = MN.$ Join EC and NR.
15. 42m

EXERCISE 7.1

1. (i) $2\sqrt{2}$ (ii) $4\sqrt{2}$ (iii) $2\sqrt{a^2+b^2}$
 2. 39; 39 km 3. No 4. Yes 5. Champa is correct.
 6. (i) Square (ii) No quadrilateral (iii) Parallelogram
 7. $(-7, 0)$ 8. $-9, 3$ 9. ± 4 , QR = $\sqrt{41}$, PR = $\sqrt{82}$, $9\sqrt{2}$
 10. $3x + y - 5 = 0$

EXERCISE 7.2

1. $(1, 3)$ 2. $\left(2, -\frac{5}{3}\right); \left(0, -\frac{7}{3}\right)$
 3. $\sqrt{61}$ m; 5th line at a distance of 22.5 m 4. 2 : 7
 5. $1 : 1; \left(-\frac{3}{2}, 0\right)$ 6. $x = 6, y = 3$ 7. $(3, -10)$
 8. $\left(-\frac{2}{7}, -\frac{20}{7}\right)$ 9. $\left(-1, \frac{7}{2}\right), (0, 5), \left(1, \frac{13}{2}\right)$ 10. 24 sq. units

EXERCISE 8.1

1. (i) $\sin A = \frac{7}{25}, \cos A = \frac{24}{25}$ (ii) $\sin C = \frac{24}{25}, \cos C = \frac{7}{25}$
 2. 0 3. $\cos A = \frac{\sqrt{7}}{4}, \tan A = \frac{3}{\sqrt{7}}$ 4. $\sin A = \frac{15}{17}, \sec A = \frac{17}{8}$
 5. $\sin \theta = \frac{5}{13}, \cos \theta = \frac{12}{13}, \tan \theta = \frac{5}{12}, \cot \theta = \frac{12}{5}, \operatorname{cosec} \theta = \frac{13}{5}$
 7. (i) $\frac{49}{64}$ (ii) $\frac{49}{64}$ 8. Yes
 9. (i) 1 (ii) 0 10. $\sin P = \frac{12}{13}, \cos P = \frac{5}{13}, \tan P = \frac{12}{5}$
 11. (i) False (ii) True (iii) False (iv) False (v) False

EXERCISE 8.2

1. (i) 1 (ii) 2 (iii) $\frac{3\sqrt{2} - \sqrt{6}}{8}$ (iv) $\frac{43 - 24\sqrt{3}}{11}$ (v) $\frac{67}{12}$
2. (i) A (ii) D (iii) A (iv) C 3. $\angle A = 45^\circ, \angle B = 15^\circ$
4. (i) False (ii) True (iii) False (iv) False (v) True

EXERCISE 8.3

$$1. \sin A = \frac{1}{\sqrt{1 + \cot^2 A}}, \tan A = \frac{1}{\cot A}, \sec A = \frac{\sqrt{1 + \cot^2 A}}{\cot A}$$

$$2. \sin A = \frac{\sqrt{\sec^2 A - 1}}{\sec A}, \cos A = \frac{1}{\sec A}, \tan A = \sqrt{\sec^2 A - 1}$$

$$\cot A = \frac{1}{\sqrt{\sec^2 A - 1}}, \operatorname{cosec} A = \frac{\sec A}{\sqrt{\sec^2 A - 1}}$$

3. (i) B (ii) C (iii) D (iv) D

EXERCISE 9.1

1. 10m 2. $8\sqrt{3}$ m 3. 3m, $2\sqrt{3}$ m 4. $10\sqrt{3}$ m
5. $40\sqrt{3}$ m 6. $19\sqrt{3}$ m 7. $20(\sqrt{3} - 1)$ m 8. $0.8(\sqrt{3} + 1)$ m
9. $16\frac{2}{3}$ m 10. $20\sqrt{3}$ m, 20m, 60m 11. $10\sqrt{3}$ m, 10m 12. $7(\sqrt{3} + 1)$ m
13. $75(\sqrt{3} - 1)$ m 14. $58\sqrt{3}$ m 15. 3 seconds

EXERCISE 10.1

1. Infinitely many
2. (i) One (ii) Secant (iii) Two (iv) Point of contact 3. D

EXERCISE 10.2

1. A 2. B 3. A 6. 3 cm
7. 8 cm 12. AB = 15 cm, AC = 13 cm

EXERCISE 11.1

1. $\frac{132}{7} \text{ cm}^2$
2. $\frac{77}{8} \text{ cm}^2$
3. $\frac{154}{3} \text{ cm}^2$
4. (i) 28.5 cm^2 (ii) 235.5 cm^2
5. (i) 22 cm (ii) 231 cm^2 (iii) $\left(231 - \frac{441\sqrt{3}}{4}\right) \text{ cm}^2$
6. 20.4375 cm^2 ; 686.0625 cm^2
7. 88.44 cm^2
8. (i) 19.625 m^2 (ii) 58.875 cm^2
9. (i) 285 mm (ii) $\frac{385}{4} \text{ mm}^2$
10. $\frac{22275}{28} \text{ cm}^2$
11. $\frac{158125}{126} \text{ cm}^2$
12. 189.97 km^2
13. ₹ 162.68
14. D

EXERCISE 12.1

1. 160 cm^2
2. 572 cm^2
3. 214.5 cm^2
4. Greatest diameter = 7 cm, surface area = 332.5 cm^2
5. $\frac{1}{4} l^2 (\pi + 24)$
6. 220 mm^2
7. 44 m^2 , ₹ 22000
8. 18 cm^2
9. 374 cm^2

EXERCISE 12.2

1. $\pi \text{ cm}^3$
2. 66 cm^3 . Volume of the air inside the model = Volume of air inside (cone + cylinder + cone)
 $= \left(\frac{1}{3} \pi r^2 h_1 + \pi r^2 h_2 + \frac{1}{3} \pi r^2 h_1 \right)$, where r is the radius of the cone and the cylinder, h_1 is the height (length) of the cone and h_2 is the height (length) of the cylinder.

$$\text{Required Volume} = \frac{1}{3} \pi r^2 (h_1 + 3h_2 + h_1).$$

3. 338 cm^3
4. 523.53 cm^3
5. 100
6. 892.26 kg
7. 1.131 m^3 (approx.)
8. Not correct. Correct answer is 346.51 cm^3 .

EXERCISE 13.1

- 8.1 plants. We have used direct method because numerical values of x_i and f_i are small.
- ₹ 545.20
- $f = 20$
- 75.9
- 57.19
- ₹ 211
- 0.099 ppm
- 12.48 days
- 69.43 %

EXERCISE 13.2

- Mode = 36.8 years, Mean = 35.37 years. Maximum number of patients admitted in the hospital are of the age 36.8 years (approx.), while on an average the age of a patient admitted to the hospital is 35.37 years.
- 65.625 hours
- Modal monthly expenditure = ₹ 1847.83, Mean monthly expenditure = ₹ 2662.5.
- Mode : 30.6, Mean = 29.2. Most states/U.T. have a student teacher ratio of 30.6 and on an average, this ratio is 29.2.
- Mode = 4608.7 runs
- Mode = 44.7 cars

EXERCISE 13.3

- Median = 137 units, Mean = 137.05 units, Mode = 135.76 units.
The three measures are approximately the same in this case.
- $x = 8, y = 7$
- Median age = 35.76 years
- Median length = 146.75 mm
- Median life = 3406.98 hours
- Median = 8.05, Mean = 8.32, Modal size = 7.88
- Median weight = 56.67 kg

EXERCISE 14.1

- (i) 1 (ii) 0, impossible event (iii) 1, sure or certain event
(iv) 1 (v) 0, 1
- The experiments (iii) and (iv) have equally likely outcomes.
- When we toss a coin, the outcomes head and tail are equally likely. So, the result of an individual coin toss is completely unpredictable.
- B
- 0.95
- (i) 0 (ii) 1
- 0.008
- (i) $\frac{3}{8}$ (ii) $\frac{5}{8}$
- (i) $\frac{5}{17}$ (ii) $\frac{8}{17}$ (iii) $\frac{13}{17}$
- (i) $\frac{5}{9}$ (ii) $\frac{17}{18}$

EXERCISE A1.1

- (i) Ambiguous (ii) True (iii) True (iv) Ambiguous
(v) Ambiguous
- (i) True (ii) True (iii) False (iv) True (v) True
- Only (ii) is true.
- (i) If $a > 0$ and $a^2 > b^2$, then $a > b$.
(ii) If $xy \geq 0$ and $x^2 = y^2$, then $x = y$.
(iii) If $(x + y)^2 = x^2 + y^2$ and $y \neq 0$, then $x = 0$.
(iv) The diagonals of a parallelogram bisect each other.

EXERCISE A1.2

- A is mortal
- ab is rational
- Decimal expansion of $\sqrt{17}$ is non-terminating non-recurring.
- $y = 7$
- $\angle A = 100^\circ, \angle C = 100^\circ, \angle D = 180^\circ$
- PQRS is a rectangle.
- Yes, because of the premise. No, because $\sqrt{3721} = 61$ which is not irrational. Since the premise was wrong, the conclusion is false.

EXERCISE A1.3

- Take two consecutive odd numbers as $2n + 1$ and $2n + 3$ for some integer n .

EXERCISE A1.4

- (i) Man is not mortal.
(ii) Line l is not parallel to line m .
(iii) The chapter does not have many exercises.
(iv) Not all integers are rational numbers.
(v) All prime numbers are not odd.
(vi) Some students are lazy.
(vii) All cats are black.
(viii) There is at least one real number x , such that $\sqrt{x} = -1$.

- (ix) 2 does not divide the positive integer a .
 (x) Integers a and b are not coprime.
2. (i) Yes (ii) No (iii) No (iv) No (v) Yes

EXERCISE A1.5

- If Sharan sweats a lot, then it is hot in Tokyo.
 - If Shalini's stomach grumbles, then she is hungry.
 - If Jaswant can get a degree, then she has a scholarship.
 - If a plant is alive, then it has flowers.
 - If an animal has a tail, then it is a cat.
- If the base angles of triangle ABC are equal, then it is isosceles. True.
 - If the square of an integer is odd, then the integer is odd. True.
 - If $x = 1$, then $x^2 = 1$. True.
 - If AC and BD bisect each other, then ABCD is a parallelogram. True.
 - If $a + (b + c) = (a + b) + c$, then a , b and c are whole numbers. False.
 - If $x + y$ is an even number, then x and y are odd. False.
 - If a parallelogram is a rectangle, its vertices lie on a circle. True.

EXERCISE A1.6

- Suppose to the contrary $b \leq d$.
- See Example 10 of Chapter 1.
- See Theorem 5.1 of Class IX Mathematics Textbook.

EXERCISE A2.2

- $\frac{1}{5}$
 - 160
- Take 1 cm^2 area and count the number of dots in it. Total number of trees will be the product of this number and the area (in cm^2).
- Rate of interest in instalment scheme is 17.74 %, which is less than 18 %.

EXERCISE A2.3

- Students find their own answers.